

(3.3) Assuming that in the fission of a uranium atom an energy amount of 200 MeV is released, how far would 1 g of  $^{235}\text{U}$  drive a car which consumes 1 liter of gasoline (density  $0.70 \text{ g cm}^{-3}$ ) for each 10 km? The combustion heat of octane is  $5500 \text{ kJ mole}^{-1}$ , and the combustion engine has an efficiency of 18%.

We assume 100% efficiency for energy from uranium. In reality it would probably be more like the ~35% achieved in nuclear ships.

The molar weight of n-octane ( $\text{C}_8\text{H}_{18}$ ) can be estimated as:

$$\begin{aligned} \text{MeV} &:= 1.60217733 \cdot 10^{-13} \cdot \text{joule} & M_{\text{C}} &:= 12.01 \cdot \text{gm} \cdot \text{mole}^{-1} & M_{\text{H}} &:= 1.008 \cdot \text{gm} \cdot \text{mole}^{-1} \\ M_{\text{oct}} &:= 8 \cdot M_{\text{C}} + 18 \cdot M_{\text{H}} & M_{\text{oct}} &= 114.224 \cdot \text{gm} \cdot \text{mole}^{-1} \end{aligned}$$

Its combustion energy,  $H_{\text{oct}}$ , is then:

$$\begin{aligned} H_{\text{comb}} &:= 5500 \cdot 10^3 \cdot \text{joule} \cdot \text{mole}^{-1} & \rho_{\text{oct}} &:= 0.7 \cdot \text{gm} \cdot \text{mL}^{-1} \\ H_{\text{oct}} &:= \frac{\rho_{\text{oct}} H_{\text{comb}}}{M_{\text{oct}}} & H_{\text{oct}} &= 3.371 \cdot 10^7 \cdot \text{joule} \cdot \text{liter}^{-1} \quad (1 \text{ liter can move the car } 10 \text{ km}) \end{aligned}$$

Approximating the fission energy of 1  $^{235}\text{U}$  atom by 200 MeV, eqn. (19.1) on p. 518, the nuclear energy,  $Q$ , is:

$$\begin{aligned} M_{\text{U235}} &:= 235 \cdot \text{gm} \cdot \text{mole}^{-1} & N_{\text{A}} &:= 6.0221367 \cdot 10^{23} \cdot \text{mole}^{-1} & Q_{\text{fiss}} &:= 200 \cdot \text{MeV} \\ Q &:= Q_{\text{fiss}} \cdot \frac{1}{M_{\text{U235}}} \cdot N_{\text{A}} & Q &= 8.212 \cdot 10^{10} \cdot \text{joule} \cdot \text{gm}^{-1} & H_{\text{oct}} &= 3.371 \cdot 10^7 \cdot \text{joule} \cdot \text{liter}^{-1} \\ \text{dist} &:= \frac{1 \cdot \text{gm} \cdot Q}{1 \cdot \text{liter} \cdot H_{\text{oct}} \cdot 0.18} \cdot 10 \cdot \text{km} & \text{dist} &= 135347 \cdot \text{km} \end{aligned}$$

(In case we use the nuclear thermal efficiency typical for nuclear ships, 35%, we would get:

$$\frac{1 \cdot \text{gm} \cdot Q \cdot 0.35}{1 \cdot \text{liter} \cdot H_{\text{oct}} \cdot 0.18} \cdot 10 \cdot \text{km} = 4737 \cdot \text{km}$$