

(6.9) In a laboratory an irradiation area must be designed for  $\gamma$ -radiography using a 0.37 TBq  $^{60}\text{Co}$  source. For this purpose a cubic building is erected with an interior side length of 2 m. The desired flux reduction is  $10^6$ . How thick must the wall be and how much will the shielding material cost (i.e. not including labor costs) if it is made of (a) concrete? (b) lead ? Assume lead blocks cost \$1.50 per kg and concrete \$40 per  $\text{m}^3$ .

From Fig. 6.15 and  $E_\gamma$  1.17 and 1.33; average 1.25 MeV, the thickness  $d_{\text{concrete}}$  is obtained as:

$$d_{\text{concrete}} := 133 \cdot 10^{-2} \cdot \text{m}$$

The concrete volume is calculated as the difference in volume between a massive cube and a hollow cube having outer dimension = inner dimension + wall thickness.

$$\text{Volume} := (2 \cdot \text{m} + 2 \cdot d_{\text{concrete}})^3 - (2 \cdot \text{m})^3 \quad \text{Volume} = 93.195 \cdot \text{m}^3$$

$$\text{Unitcost} := 40 \cdot \text{m}^{-3} \quad \text{in } \$/\text{m}^3$$

$$\text{Cost} := \text{Volume} \cdot \text{Unitcost} \quad \text{Cost} = 3.728 \cdot 10^3 \quad \$ \text{ for concrete}$$

From Fig. 6.17 we can read the total attenuation coefficient for lead as  $\mu = 0.059 \text{ cm}^2/\text{g}$  at 1.25 MeV:

$$\rho_{\text{Pb}} := 11.3 \cdot \frac{\text{gm}}{\text{cm}^3} \quad \mu_o := 0.059 \cdot \frac{\text{cm}^2}{\text{gm}} \quad \mu := \mu_o \cdot \rho_{\text{Pb}}$$

However, in this case we must also correct for scattered radiation by using the build-up factor,  $B$ , because the attenuation was measured on a collimated beam:

$$\phi = \phi_o \cdot B \cdot e^{-\mu \cdot x} \quad \text{which can be solved for } \mu \cdot x \quad \mu \cdot x = \ln\left(\frac{\phi_o}{\phi} \cdot B\right)$$

$$B := 1.0 \quad \text{a first guess:} \quad x\mu := \ln(10^6 \cdot B)$$

$$x\mu = 13.816$$

$$B := 5 \quad \text{From Fig. 6.20; second guess.}$$

$$x\mu := \ln(10^6 \cdot B) \quad x\mu = 15.425$$

$$B := 5.5 \quad \text{From Fig. 6.20}$$

$$x\mu := \ln(10^6 \cdot B) \quad x\mu = 15.52 \quad \text{Change in } \mu x \text{ is small, so } B=5.5 \text{ is OK}$$

$$x := \frac{x\mu}{\mu} \quad x = 0.233 \cdot \text{m}$$

$$\text{Volume}_{\text{Pb}} := (2 \cdot \text{m} + 2 \cdot x)^3 - (2 \cdot \text{m})^3 \quad \text{Volume}_{\text{Pb}} = 6.989 \cdot \text{m}^3$$

$$\text{Unitcost} := 1.50 \cdot \text{kg}^{-1} \quad \text{in } \$/\text{kg}$$

$$\text{Cost}_{\text{Pb}} := \text{Volume}_{\text{Pb}} \cdot \text{Unitcost} \cdot \rho_{\text{Pb}} \quad \text{Cost}_{\text{Pb}} = 1.185 \cdot 10^5 \quad \$ \text{ for Pb}$$