

(7.1) How many ion pairs are produced in 10 m of air of STP by one (a) 5 MeV α -particle, (b) 1 MeV β -particle and (c) 1 MeV γ -quantum ($\mu_m(\text{air}) = \mu_m(\text{water})$)?

First we need to define the electron volt and MeV as:

$$eV := 1.60217733 \cdot 10^{-19} \cdot \text{joule} \quad MeV := 10^6 \cdot eV$$

The ionization energy, eV/ion pair, is taken from Table 7.1: $w := 34 \cdot eV$

(a) The range of a 5 MeV α -particle is $\ll 10$ m, hence all energy will be used for ionization:

$$E_\alpha := 5 \cdot MeV \quad \text{Hence} \quad n := \frac{E_\alpha}{w} \quad n = 1.471 \cdot 10^5 \quad \text{ion pairs}$$

(b) The range of a 1 MeV β -particle is < 10 m, hence all energy will be used for ionization:

$$E_\beta := 1 \cdot MeV \quad \text{Hence} \quad n := \frac{E_\beta}{w} \quad n = 2.941 \cdot 10^4 \quad \text{ion pairs}$$

(c) The γ passes 10 m of air, hence only part of the energy will be deposited and form ion pairs. The value for $\mu_m(\text{water})$ can be read from Fig. 6.17:

$$E_\gamma := 1 \cdot MeV \quad \mu_{mair} := 0.026 \cdot \frac{cm^2}{gm} \quad \rho_{air} := 1.293 \cdot 10^{-3} \cdot \frac{gm}{cm^3}$$

$$\mu_{air} := \mu_{mair} \cdot \rho_{air}$$

Linear absorption coefficient

$$x := 10 \cdot m$$

Length of the air path

$$I_0 := 1$$

Assume one unit of incoming intensity

$$I := I_0 \cdot \exp(-\mu_{air} \cdot x)$$

Escaping intensity, from eqn.(6.27) with $B=1$

$$E := E_\gamma (I_0 - I)$$

$$E = 3.306 \cdot 10^4 \cdot eV$$

Deposited energy in 10 m of air

Hence

$$n := \frac{E}{w}$$

$$n = 972 \quad \text{ion pairs}$$