

(7.4) An acidic aqueous solution is irradiated by  $\alpha$ -particles from dissolved  $^{239}\text{Pu}$  at a concentration of 0.03 M. The plutonium is originally in the in its hexavalent state, but is reduced to the tertavalent state by the reaction  $\text{Pu(VI)} + 2\text{H} \rightarrow \text{Pu(IV)} + 2\text{H}^+$ . How much of the plutonium can be reduced in one week?

Constants and units:

$$N_A := 6.0221367 \cdot 10^{23} \cdot \text{mole}^{-1} \quad \text{eV} := 1.60217733 \cdot 10^{-19} \cdot \text{joule} \quad \text{keV} := 10^3 \cdot \text{eV}$$

$$\mu\text{m} := 10^{-6} \cdot \text{m} \quad \text{\AA} := 10^{-8} \cdot \text{cm} \quad \text{Bq} := \text{sec}^{-1} \quad M := \text{mole} \cdot \text{liter}^{-1}$$

Average LET value is interpolated from Table 6.2 for 5.157 MeV  $\alpha$  from  $^{239}\text{Pu}$  as follows:

$$i := 1 \dots 3$$

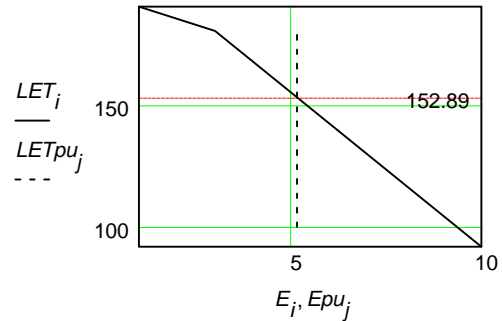
$$j := 1 \dots 2$$

$$E_i := \quad \text{LET}_i :=$$

1	190
3	180
10	92

$$E_{pu_j} := \quad \text{LET}_{pu_j} :=$$

5.157	100
5.158	180



$$\text{LET} := 152.891 \cdot \text{keV} \cdot \mu\text{m}^{-1} \quad \text{LET} = 15.289 \cdot \frac{\text{eV}}{\text{\AA}}$$

This LET value gives a G-value for H $\cdot$  from Fig. 7.6 of:

$$G := 0.25 \cdot 10^{-7} \cdot \text{mole} \cdot \text{joule}^{-1}$$

$$t_{\text{half}} := 2.411 \cdot 10^4 \cdot \text{yr} \quad E_{\alpha} := 5.158 \cdot 10^6 \cdot \text{eV}$$

$$C_{Pu} := 0.03 \cdot M$$

$$N_{Pu} := C_{Pu} \cdot N_A$$

$$R_{Pu} := N_{Pu} \cdot \frac{\ln(2)}{t_{\text{half}}}$$

$$dDdt := R_{Pu} \cdot E_{\alpha}$$

$$t := 7 \cdot \text{day} \quad dC := t \cdot \frac{dDdt}{2} \cdot G \quad (2 \text{ H} \cdot \text{ for each Pu}) \quad dC = 1.028 \cdot 10^{-4} \cdot M$$

$$dC_{\text{rel}} := \frac{dC}{C_{Pu}}$$

$$dC_{\text{rel}} = 3.428 \cdot 10^{-3}$$

$$dC_{\text{rel}} = 0.343 \cdot \%$$