

(8.2) A ~ 100 MeV fission fragment is stopped in a plastic plate with density ~ 1 and an average atomic spacing of 0.25 nm. Estimate (a) the range in the plate, and (b) the ionization density (ion pairs mm^{-1}). If the ionization along the track is spread out perpendicular from the track so that 1 in 10 atoms are ionized (c) what would be the diameter of the track? From the track dimensions (d) calculate the average energy deposition to each atom within the "cylinder", and, using the relation $E=3kT/2$, (e) estimate the average temperature within the track volume. In lack of basic data for the plastic material, use data for water.

First we must define units:

$$\mu\text{m} := 10^{-6} \cdot \text{m} \quad \text{eV} := 1.60217733 \cdot 10^{-19} \cdot \text{joule} \quad \text{nm} := 10^{-9} \cdot \text{m}$$

$$\text{(a)} \quad \text{Range} := 0.025 \cdot \text{mm} \quad (\text{from Table 6.2}) \quad \text{Range} = 25 \cdot \mu\text{m}$$

$$\text{(b)} \quad E := 100 \cdot 10^6 \cdot \text{eV} \quad w := 38 \cdot \text{eV} \quad \text{eV/ion pair (from Table 7.1)}$$

$$\text{LET} := \frac{E}{w \cdot \text{Range}} \quad \text{LET} = 1.053 \cdot 10^5 \cdot \mu\text{m}^{-1} \quad \text{ion pairs}/\mu\text{m}$$

$$\text{(c)} \quad n := \frac{E}{w} \quad \text{ion pairs totally} \quad N := 10 \cdot n \quad \text{atoms in track}$$

$$\text{volume} := N \cdot (0.25 \cdot \text{nm})^3 \quad \text{length} := \text{Range} \quad \text{section} := \frac{\text{volume}}{\text{length}}$$

$$\text{radius} := \sqrt{\frac{\text{section}}{\pi}} \quad \text{diameter} := 2 \cdot \text{radius} \quad \text{diameter} = 4.576 \cdot \text{nm}$$

$$\text{(d)} \quad 1 \text{ atoms in } 10 \text{ is ionized at } 38 \text{ eV, thus: } E_{\text{avg}} := \frac{w}{10} \quad E_{\text{avg}} = 3.8 \cdot \text{eV} \quad \text{eV/atom}$$

(e) From this excitation energy and using $E=3kT/2$, eqn. (2.21), we get:

$$k := 8.61739 \cdot 10^{-5} \cdot \frac{\text{eV}}{\text{K}} \quad T := \frac{2}{3} \cdot \frac{E_{\text{avg}}}{k} \quad T = 2.94 \cdot 10^4 \cdot \text{K}$$