

(12.1) (a) What kinetic energy must be given to a helium atom in order to increase its mass by 1%? (b) What are the mean velocity and the mean kinetic energy of a helium atom at STP?

First a definition of eV:

$$eV := 1.60217733 \cdot 10^{-19} \cdot \text{joule}$$

(a) Eqn. (12.7) can be rewritten as $E_{\text{kin}} = (m - m^0) \cdot c^2$ by using (12.5) and (12.6). If we convert to the amu scale the eqn. becomes $E_{\text{kin}} = 931.5 \cdot \Delta M$ for E_{kin} in MeV and ΔM in u.

$$\Delta M := \frac{1}{100} \cdot 4.002603 \quad \text{This is 1\% of the rest mass of a helium atom.}$$

$$E_{\text{kin}} := 931.5 \cdot \Delta M \quad E_{\text{kin}} = 37.3 \quad \text{MeV}$$

(b) From eqns (2.21) and (2.24) we obtain:

$$k := 1.38066 \cdot 10^{-23} \cdot \frac{\text{joule}}{K} \quad T := 273.15 \cdot K$$

$$E_{\text{mean}} := \frac{3 \cdot k \cdot T}{2} \quad E_{\text{mean}} = 5.657 \cdot 10^{-21} \cdot \text{joule} \quad \text{or} \quad E_{\text{mean}} = 0.035 \cdot eV$$

$$m_{\text{He}} := 4.002603 \cdot 1.660540 \cdot 10^{-27} \cdot \text{kg}$$

$$v_{\text{mean}} := \sqrt{\frac{2 \cdot E_{\text{mean}}}{m_{\text{He}}}}$$

$$v_{\text{mean}} = 1305 \cdot \text{m} \cdot \text{sec}^{-1}$$