

(15.1) ^{24}Na is produced through the reaction $^{26}\text{Mg}(\text{d},\alpha)^{24}\text{Na}$. A 0.2 mm thick magnesium foil is irradiated for 1 h by a current of 130 μA of 22 MeV D^+ ions in a cyclotron. The foil has a much larger area than the cross-section of the beam. What is the specific activity of ^{24}Na if the magnesium foil (3 cm^2) contains 0.003% Na and σ for the reaction is assumed to be 25 mb?

First the usual definition of units and constants:

$$\begin{aligned} q_e &:= 1.6021773 \cdot 10^{-19} \cdot \text{coul} & N_A &:= 6.022137 \cdot 10^{23} \cdot \text{mole}^{-1} & \text{Bq} &:= \text{sec}^{-1} \\ \text{kBq} &:= 1000 \cdot \text{Bq} & \text{MBq} &:= 1000 \cdot \text{kBq} & \text{GBq} &:= 1000 \cdot \text{MBq} & \text{TBq} &:= 1000 \cdot \text{GBq} \\ \text{PBq} &:= 1000 \cdot \text{TBq} & \text{EBq} &:= 1000 \cdot \text{PBq} \end{aligned}$$

Then the values given in the text, etc.:

$$\begin{aligned} M_{\text{Mg}} &:= 24.31 \cdot \text{gm} \cdot \text{mole}^{-1} & \rho_{\text{Mg}} &:= 1.74 \cdot \text{gm} \cdot \text{cm}^{-3} & y_{^{26}\text{Mg}} &:= 11 \cdot \% \\ x &:= 0.2 \cdot \text{mm} & t_{\text{irr}} &:= 1 \cdot \text{hr} & I_D &:= 130 \cdot \mu\text{A} & \sigma &:= 25 \cdot 10^{-3} \cdot 10^{-28} \cdot \text{m}^2 \\ t_{\text{half}} &:= 14.96 \cdot \text{hr} & \text{area} &:= 3 \cdot \text{cm}^2 & c_{\text{Na}} &:= 0.003 \cdot \% \end{aligned}$$

Calculations:

$$\phi := \frac{I_D}{1 \cdot q_e} \quad \lambda := \frac{\ln(2)}{t_{\text{half}}} \quad N_{\text{vX}} := \frac{\rho_{\text{Mg}} \cdot x \cdot y_{^{26}\text{Mg}}}{M_{\text{Mg}}} \cdot N_A$$

$$R_{^{24}\text{Na}} := \phi \cdot \sigma \cdot N_{\text{vX}} \left(1 - \exp(-t_{\text{irr}} \cdot \lambda) \right) \quad \text{eqn. (15.9) with } t_{\text{cool}} = 0$$

$$\text{volume} := x \cdot \text{area} \quad \text{mass} := \rho_{\text{Mg}} \cdot \text{volume} \quad \text{weight}_{\text{Na}} := c_{\text{Na}} \cdot \text{mass}$$

$$S_{\text{Na}} := \frac{R_{^{24}\text{Na}}}{\text{weight}_{\text{Na}}} \quad S_{\text{Na}} = 28 \cdot \frac{\text{PBq}}{\text{kg}} \quad \text{Answer: } 28 \text{ PBq/kg Na}$$