

(3.5) In a Dempster type (constant  $B$  and  $V$ ) type spectrograph utilising 180 degree focusing, the ions  $^{12}\text{C}^+$  and  $^{11}\text{BH}^+$  are recorded simultaneously, the latter ion having a slightly larger orbit diameter. The separation between the lines recorded on the photographic plate is 0.0143 cm and the orbit diameter for the  $^{12}\text{C}^+$  ion is 20 cm. What is the atomic mass of  $^{11}\text{B}$ ?

Designate the orbit diameter for ion no 1 by  $r$  and the separation to the second ion by  $x$ . Then eqn. (3.12) gives the following relation when applied to both ion no 1 and ion no 2:

$$m_1 = q_1 \cdot r^2 \cdot B^2 / 2 \cdot V \quad \text{and} \quad m_2 = q_2 \cdot (r+x)^2 \cdot B^2 / 2 \cdot V; \quad \text{hence by division} \quad m_2 / m_1 = (q_2 / q_1) \cdot ((r+x) / r)^2 = M_2 / M_1$$

$$amu := 1.6605402 \cdot 10^{-27} \cdot kg$$

$$M_e := 5.485799 \cdot 10^{-4} \cdot amu$$

The mass of an electron is  $M_e$

$$r := \frac{20}{2} \cdot 0.01 \cdot m$$

$$M_1 := 12 \cdot amu - M_e$$

Because the  $^{12}\text{C}$ -ion lacks 1 electron

$$x := \frac{0.0143}{2} \cdot 0.01 \cdot m$$

$$q_1 := 1$$

$$q_2 := 1$$

$$M_2 := M_1 \cdot \left( \frac{q_2}{q_1} \right) \cdot \left( \frac{r+x}{r} \right)^2$$

$$M_2 = 12.016617 \cdot amu$$

The mass of  $\text{BH}^+$  ions

In order to obtain the mass of the  $^{11}\text{B}$ -atom we must subtract the mass of a  $\text{H}^+$  ion as follows:

$$M_H := 1.007825 \cdot amu$$

$$M_B := M_2 - (M_H - M_e)$$

$$M_B = 1.82815 \cdot 10^{-26} \cdot kg$$

or

$$M_B = 11.00934 \cdot amu$$