

(4.3) Assuming that in the fission of a uranium atom an energy amount of 200 MeV is released, how far would 1 g of  $^{235}\text{U}$  drive a car which consumes 1 liter of gasoline (density  $0.70 \text{ g cm}^{-3}$ ) for each 10 km? The combustion heat of octane is  $5500 \text{ kJ mole}^{-1}$ , and the combustion engine has an efficiency of 18%.

We assume 100% efficiency for energy from uranium. In reality it would probably be more like the ~35% achieved in nuclear ships.

The molar weight of n-octane ( $\text{C}_8\text{H}_{18}$ ) can be estimated as:

$$M_{\text{eV}} := 1.60217733 \cdot 10^{-13} \cdot \text{joule} \quad M_{\text{C}} := 12.01 \cdot \text{gm} \cdot \text{mole}^{-1} \quad M_{\text{H}} := 1.008 \cdot \text{gm} \cdot \text{mole}^{-1}$$

$$M_{\text{oct}} := 8 \cdot M_{\text{C}} + 18 \cdot M_{\text{H}} \quad M_{\text{oct}} = 114.224 \cdot \text{gm} \cdot \text{mole}^{-1}$$

Its combustion energy,  $H_{\text{oct}}$ , is then:

$$H_{\text{comb}} := 5500 \cdot 10^3 \cdot \text{joule} \cdot \text{mole}^{-1} \quad \rho_{\text{oct}} := 0.7 \cdot \text{gm} \cdot \text{mL}^{-1}$$

$$H_{\text{oct}} := \frac{\rho_{\text{oct}} H_{\text{comb}}}{M_{\text{oct}}} \quad H_{\text{oct}} = 3.371 \cdot 10^7 \cdot \text{joule} \cdot \text{liter}^{-1} \quad (\text{1 liter can move the car 10 km})$$

Approximating the fission energy of 1  $^{235}\text{U}$  atom by 200 MeV, eqn. (19.1), the nuclear energy,  $Q$ , is:

$$M_{\text{U235}} := 235 \cdot \text{gm} \cdot \text{mole}^{-1} \quad N_{\text{A}} := 6.0221367 \cdot 10^{23} \cdot \text{mole}^{-1} \quad Q_{\text{fiss}} := 200 \cdot \text{MeV}$$

$$Q := Q_{\text{fiss}} \cdot \frac{1}{M_{\text{U235}}} \cdot N_{\text{A}} \quad Q = 8.212 \cdot 10^{10} \cdot \text{joule} \cdot \text{gm}^{-1} \quad H_{\text{oct}} = 3.371 \cdot 10^7 \cdot \text{joule} \cdot \text{liter}^{-1}$$

$$\text{dist} := \frac{1 \cdot \text{gm} \cdot Q}{1 \cdot \text{liter} \cdot H_{\text{oct}} \cdot 0.18} \cdot 10 \cdot \text{km} \quad \text{dist} = 135347 \cdot \text{km}$$

(In case we use the nuclear thermal efficiency producing electricity, 35%, we would instead get:

$$\frac{1 \cdot \text{gm} \cdot Q \cdot 0.35}{1 \cdot \text{liter} \cdot H_{\text{oct}} \cdot 0.18} \cdot 10 \cdot \text{km} = 47371 \cdot \text{km} )$$