

(6.10) A γ -line at 0.146 MeV is assigned to a +4 to +0 rotational level change in ^{238}Pu . (a) What should the energy of the +2 and +6 rotational levels be? Compare with the measured values of 0.044 and 0.304 MeV. (b) If ^{238}Pu is considered to be a homogenous sphere, what will its apparent radius be? Compare with that obtained using relation (4.14)

$$E_{\text{rot}} = \left(\frac{h}{2\pi} \right)^2 / (2I_{\text{rot}}) \cdot n_r \cdot (n_r + 1). \text{ Hence } I_{\text{rot}} = \left(\frac{h}{2\pi} \right)^2 / (2E_{\text{rot}}) \cdot n_r \cdot (n_r + 1)$$

(a).

$$\text{MeV} := 10^6 \cdot 1.602177 \cdot 10^{-19} \cdot \text{joule}$$

$$h := 6.626076 \cdot 10^{-34} \cdot \text{joule} \cdot \text{sec} \quad E_{\text{rot}} := 0.146 \cdot \text{MeV} \quad n_r := 4$$

$$I_{\text{rot}} := \frac{\left(\frac{h}{2\pi} \right)^2}{2 \cdot E_{\text{rot}}} \cdot n_r \cdot (n_r + 1) \quad I_{\text{rot}} = 4.754 \cdot 10^{-54} \cdot \text{kg} \cdot \text{m}^2$$

$$A := 238 \quad Z := 94 \quad N := A - Z$$

$$n := 0, 2..6$$

$$E_n := \frac{\left(\frac{h}{2\pi} \right)^2}{2 \cdot I_{\text{rot}}} \cdot n \cdot (n + 1)$$

$$E\gamma_n := \frac{E_n}{1.602177 \cdot 10^{-19}} \cdot 10^{-6}$$

E_n	n	$E\gamma_n$	
$0 \cdot \text{kg} \cdot \text{m}^2 \cdot \text{sec}^{-2}$	0	$0 \cdot \text{kg} \cdot \text{m}^2 \cdot \text{sec}^{-2}$	
$7.018 \cdot 10^{-15} \cdot \text{kg} \cdot \text{m}^2 \cdot \text{sec}^{-2}$	2	$0.044 \cdot \text{kg} \cdot \text{m}^2 \cdot \text{sec}^{-2}$	+2 level 0.044 MeV
$2.339 \cdot 10^{-14} \cdot \text{kg} \cdot \text{m}^2 \cdot \text{sec}^{-2}$	4	$0.146 \cdot \text{kg} \cdot \text{m}^2 \cdot \text{sec}^{-2}$	+4 level 0.146 MeV
$4.912 \cdot 10^{-14} \cdot \text{kg} \cdot \text{m}^2 \cdot \text{sec}^{-2}$	6	$0.307 \cdot \text{kg} \cdot \text{m}^2 \cdot \text{sec}^{-2}$	+6 level 0.307 MeV

(b) eqn (3.29): $I_{\text{rot}} = m \cdot r^2$, hence $r = \text{sqrt}(I_{\text{rot}}/m)$

$$u := 1.660540 \cdot 10^{-27} \cdot \text{kg}$$

$$m_{238\text{Pu}} := A \cdot u \quad r_{238\text{Pu}} := \sqrt{\frac{I_{\text{rot}}}{m_{238\text{Pu}}}}$$

$$r_{238\text{Pu}} = 3.468 \cdot 10^{-15} \cdot \text{m}$$

Compare with result from 4.14: $r = r_0 \cdot A^{1/3}$

$$r_0 := 1.4 \cdot 10^{-15} \cdot \text{m}$$

$$r_A := r_0 \cdot A^{1/3}$$

$$r_A = 8.676 \cdot 10^{-15} \cdot \text{m}$$