

(8.3) A freshly prepared small source of ^{24}Ne had a measured decay rate of 1 GBq 1 s after its preparation. The source is shielded by 10 cm of Pb. ^{24}Ne emits γ -rays; 8% with 0.878 MeV and 100% with 0.478 MeV. Estimate the total integrated dose received at 2 m distance during its life-time after preparation. Neglect build-up factors.

$$\begin{aligned}
 Bq &:= \text{sec}^{-1} & Gy &:= \text{joule} \cdot \text{kg}^{-1} \\
 t_{\text{half}} &:= 3.38 \cdot \text{min} & t_0 &:= 1 \cdot \text{sec} & R_1 &:= 1 \cdot 10^9 \cdot Bq \\
 \lambda &:= \frac{\ln(2)}{t_{\text{half}}} & R_0 &:= R_1 \cdot \exp(t_0 \lambda) & \text{Bq at } t=0 & R_0 = 1.003 \cdot 10^9 \cdot Bq \quad \text{at } t=0 \\
 \rho &:= 11.34 \cdot \text{gm} \cdot \text{cm}^{-3} & d &:= 10 \cdot \text{cm} & x &:= 2 \cdot \text{m} \\
 \mu_{m1} &:= 0.075 \cdot \text{cm}^2 \cdot \text{gm}^{-1} & \mu_1 &:= \mu_{m1} \rho & I_1 &:= 8 \cdot \% & \text{For the 0.878 MeV } \gamma\text{-rays} \\
 \mu_{m2} &:= 0.16 \cdot \text{cm}^2 \cdot \text{gm}^{-1} & \mu_2 &:= \mu_{m2} \rho & I_2 &:= 100 \cdot \% & \text{For the 0.478 MeV } \gamma\text{-rays} \\
 k_1 &:= 3.2 \cdot 10^{-18} \cdot \text{Gy} \cdot \text{m}^2 \cdot \text{Bq}^{-1} \cdot \text{sec}^{-1} & & & & & \text{From Fig. 8.2 for 0.878 MeV} \\
 k_2 &:= 2.7 \cdot 10^{-18} \cdot \text{Gy} \cdot \text{m}^2 \cdot \text{Bq}^{-1} \cdot \text{sec}^{-1} & & & & & \text{From Fig. 8.2 for 0.478 MeV} \\
 D_{\text{rate}} &:= \left(I_1 \cdot \exp(-\mu_1 d) \cdot k_1 + I_2 \cdot \exp(-\mu_2 d) \cdot k_2 \right) \cdot \left(\frac{1}{x^2} \right) \cdot R_0 & & & & & \text{Gy/s}
 \end{aligned}$$

We can calculate the number of decays in two ways:

First by integrating over time (100000 seconds is practically infinity)

$$D_{\text{cy}} := \int_{0 \cdot \text{sec}}^{100000 \cdot \text{sec}} \exp(-\lambda \cdot t) \cdot R_0 \cdot dt \quad D := D_{\text{rate}} \cdot D_{\text{cy}} \quad D = 3.807 \cdot 10^{-12} \cdot \text{Gy}$$

Alternatively by assuming all atoms decay simultaneously at their average lifetime.

$$N_0 := \frac{1}{\lambda} \quad \text{and then} \quad D_{\text{cy}} := N_0 \quad D := D_{\text{rate}} \cdot D_{\text{cy}} \quad D = 3.807 \cdot 10^{-12} \cdot \text{Gy}$$

(This is one case where the use of lifetime instead of half-life results in a very simple calculation)