

(8.4) An acidic aqueous solution is irradiated by α -particles from dissolved ^{239}Pu at a concentration of 0.03 M. The plutonium is originally in its hexavalent state, but is reduced to the trivalent state by the reaction $\text{Pu(VI)} + 2\text{H}^+ = \text{Pu(IV)} + 2\text{H}^+$. How much of the plutonium can be reduced in one week?

Average LET value interpolated from Table 7.2 for 5.157 MeV α from ^{239}Pu :

$$N_A := 6.0221367 \cdot 10^{23} \cdot \text{mole}^{-1} \quad eV := 1.60217733 \cdot 10^{-19} \cdot \text{joule} \quad keV := 10^3 \cdot eV$$

$$\mu m := 10^{-6} \cdot m$$

$$\text{\AA} := 10^{-8} \cdot cm$$

$$Bq := sec^{-1}$$

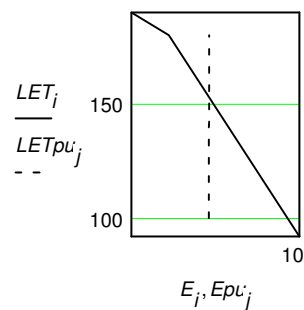
$$i := 1..3 \quad E_i := \quad LET_i := \quad j := 1..2 \quad E_{\alpha_j} := \quad LET_{\alpha_j} :=$$

1
3
10

190
180
92

5.157
5.158

100
180



$$LET := 152.891 \cdot keV \cdot \mu m^{-1}$$

$$LET = 15.289 \cdot \frac{eV}{\text{\AA}}$$

This LET value gives a G-value for H \cdot from Fig. 7.6 of:

$$G := 0.25 \cdot 10^{-7} \cdot \text{mole} \cdot \text{joule}^{-1}$$

$$t_{half} := 2.411 \cdot 10^4 \cdot yr$$

$$E_{\alpha} := 5.158 \cdot 10^6 \cdot eV$$

$$M := \text{mole} \cdot \text{liter}^{-1}$$

$$C_{Pu} := 0.03 \cdot M$$

$$N_{Pu} := C_{Pu} \cdot N_A$$

$$R_{Pu} := N_{Pu} \cdot \frac{\ln(2)}{t_{half}}$$

$$dDdt := R_{Pu} \cdot E_{\alpha}$$

$$t := 7 \cdot \text{day}$$

$$dC := t \cdot \frac{dDdt}{2} \cdot G \quad (2 \text{ H} \cdot \text{ for each Pu})$$

$$dC = 1.028 \cdot 10^{-4} \cdot M$$

$$dC_{rel} := 100 \cdot \frac{dC}{C_{Pu}}$$

$$dC_{rel} = 0.343 \quad \%$$