

(10.11) In an experiment one hopes to produce the long-lived (2.6 y)  $^{22}\text{Na}$  through a d,n-reaction on neon. What is (a) the Q-value, (b) the threshold energy, (c) the Coulomb barrier height, and (d) the minimum deuteron energy for the reaction? The mass excesses (in keV) are -5185 for  $^{22}\text{Na}$  and -8027 for  $^{22}\text{Ne}$ .

$$\text{MeV} := 1.60217733 \cdot 10^{-13} \cdot \text{joule} \quad \text{amu} := 1.6605402 \cdot 10^{-27} \cdot \text{kg}$$

$$M_n := 1.00866490 \cdot \text{amu} \quad M_d := 2.014102 \cdot \text{amu}$$

$$M_{\text{Ne}} := 22 \cdot \text{amu} - \frac{8.027 \cdot \text{MeV}}{931.5 \cdot \frac{\text{MeV}}{\text{amu}}} \quad M_{\text{Na}} := 22 \cdot \text{amu} - \frac{5.185 \cdot \text{MeV}}{931.5 \cdot \frac{\text{MeV}}{\text{amu}}}$$

(a)

$$Q := -931.5 \cdot \frac{\text{MeV}}{\text{amu}} \cdot (M_{\text{Na}} + 2 \cdot M_n - M_{\text{Ne}} - M_d) \quad Q = -9.371 \cdot 10^{-13} \cdot \text{joule} \quad Q = -5.849 \cdot \text{MeV}$$

(b)

$$E_{tr} := -Q \cdot \left( \frac{M_{\text{Na}} + M_d}{M_{\text{Na}}} \right) \quad \text{The } () \text{ contains the recoil correction} \quad E_{tr} = 6.384 \cdot \text{MeV}$$

$$(c) \quad A_1 := 2 \quad Z_1 := 1 \quad A_2 := 22 \quad Z_2 := 10$$

$$E_{cbmin} := 1.102 \cdot (A_1 + A_2) \cdot \frac{Z_1 \cdot Z_2}{A_2 \cdot \left( A_1^{\frac{1}{3}} + A_2^{\frac{1}{3}} \right)} \cdot \text{MeV} \quad E_{cbmin} = 2.96 \cdot \text{MeV}$$

(d) Because  $E_{cbmin}$  is less than  $E_{tr}$  and the change in coulomb energy is included in Q we have:

$$E_{proj} := E_{tr} \quad E_{proj} = 6.384 \cdot \text{MeV}$$