

(17.6) ^{59}Fe of high specific activity can be produced through thermal neutron irradiation of a solution of 1 ml 0.1 M potassium hexacyanoferrate. The recoiling (free) iron atoms, which are produced with a 40% yield, are quantitatively extracted into an organic solvent. How long must the irradiation be in a reactor of $3 \cdot 10^{19} \text{ n m}^{-2} \text{ s}^{-1}$ to obtain 37 MBq ^{59}Fe ? The reaction cross-section for $^{58}\text{Fe}(n,\gamma)^{59}\text{Fe}$ (β, γ 45.1 d) is 1.15 b and the isotopic abundance of ^{58}Fe is 0.3% in natural iron.

First constants and definitions:

$$N_A := 6.022137 \cdot 10^{23} \cdot \text{mole}^{-1} \quad \text{barn} := 10^{-28} \cdot \text{m}^2 \quad \text{Bq} := \text{sec}^{-1} \quad M := \text{mole} \cdot \text{liter}^{-1}$$

Then data given in the text and elsewhere:

$$t_{\text{half}} := 45.1 \cdot \text{day} \quad \lambda := \frac{\ln(2)}{t_{\text{half}}} \quad A_{^{59}\text{Fe}} := 37 \cdot 10^6 \cdot \text{Bq}$$

$$\phi := 3 \cdot 10^{19} \cdot \text{m}^{-2} \cdot \text{sec}^{-1} \quad \sigma := 1.15 \cdot \text{barn} \quad \text{volume} := 1 \cdot \text{mL}$$

$$\text{conc} := 0.1 \cdot M \quad x_{^{58}\text{Fe}} := \frac{0.3}{100} \quad \eta := \frac{40}{100}$$

Calculations (use a variant of eqn. (17.14)):

$$N_{^{58}\text{Fe}} := \text{volume} \cdot \text{conc} \cdot N_A \cdot x_{^{58}\text{Fe}} \quad N_{^{58}\text{Fe}} = 1.807 \cdot 10^{17}$$

$$t_{\text{irr}} := -\frac{1}{\lambda} \cdot \ln \left(1 - \frac{A_{^{59}\text{Fe}}}{\phi \cdot \sigma \cdot N_{^{58}\text{Fe}}} \right) \quad t_{\text{irr}} = 9.031 \cdot 10^5 \cdot \text{sec} \quad \text{or} \quad t_{\text{irr}} = 10.452 \cdot \text{day}$$