

(18.4) What is the smallest amount of indium which can be determined in a 100 mg aluminum sample using NAA with a neutron flux of  $10^{16} \text{ n m}^{-2} \text{ s}^{-1}$ ? Consider neutron captures in  $^{27}\text{Al}$  and  $^{115}\text{In}$  (95.7% of In):  $^{115}\text{In}(n,\gamma)^{116}\text{In}$  ( $\sigma$  45 b,  $t_{1/2}$  14 s) and  $^{27}\text{Al}(n,\gamma)^{28}\text{Al}$  ( $\sigma$  0.23 b,  $t_{1/2}$  2.46 min.) The lowest detectable activity of  $^{116}\text{In}$  is assumed to be 10 Bq, and the interference from  $^{28}\text{Al}$  not more than 20%.

First the standard definitions:

$$Bq := \text{sec}^{-1} \quad N_A := 6.022 \cdot 10^{23} \cdot \text{mole}^{-1}$$

then the data given in the text:

$$m_{tot} := 100 \cdot 10^{-3} \cdot \text{gm} \quad \phi := 10^{16} \cdot \text{m}^{-2} \cdot \text{sec}^{-1} \quad \sigma_{27Al} := 0.23 \cdot 10^{-28} \cdot \text{m}^2$$

$$\sigma_{115In} := 45 \cdot 10^{-28} \cdot \text{m}^2 \quad R_{116In} := 10 \cdot Bq \quad R_{28Al} := \frac{20}{100} \cdot R_{116In}$$

$$t_{half116In} := 14 \cdot \text{sec} \quad t_{half28Al} := 2.46 \cdot 60 \cdot \text{sec}$$

$$\lambda_{116In} := \frac{\ln(2)}{t_{half116In}} \quad \lambda_{28Al} := \frac{\ln(2)}{t_{half28Al}}$$

$$m_{28Al} := m_{tot} \quad \text{Neglect the small amount of In}$$

$$M_{wAl} := 26.98 \cdot \frac{\text{gm}}{\text{mole}} \quad M_{wIn} := 114.82 \cdot \frac{\text{gm}}{\text{mole}} \quad x_{In} := \frac{95.7}{100}$$

Compute the irradiation time from the requirement that  $^{28}\text{Al}$  activity is = 20% of  $^{116}\text{In}$  activity.

$$N_{27Al} := \frac{m_{tot}}{M_{wAl}} \cdot N_A \quad t_{irr} := \frac{-\ln\left(1 - \frac{R_{28Al}}{\phi \sigma_{27Al} N_{27Al}}\right)}{\lambda_{28Al}} \quad t_{irr} = 8.296 \cdot 10^{-7} \cdot \text{sec}$$

Then compute the amount of In from the required activity.

$$N_{115In} := \frac{R_{116In}}{\phi \sigma_{115In} (1 - \exp(-\lambda_{116In} t_{irr}))} \quad N_{115In} = 5.41 \cdot 10^{18}$$

$$m_{In} := N_{115In} \cdot \frac{M_{wIn}}{N_A \cdot x_{In}} \quad m_{In} = 1.078 \cdot 10^{-6} \cdot \text{kg} \quad 100 \cdot \frac{m_{In}}{m_{tot}} = 1.078 \quad \%$$

Comment: the irradiation time becomes unrealistically short at the minimum detectable activity and the sensitivity is practically constant up to near 1 second irradiation time, see next page. Thus it is more reasonable to assume  $10^7 \text{ Bq}$  of  $^{116}\text{In}$  and calculate a new irradiation time:

$$R_{116In} := 10^7 \cdot Bq \quad R_{28Al} := \frac{20}{100} \cdot R_{116In}$$

$$t_{irr} := \frac{-\ln\left(1 - \frac{R_{28Al}}{\phi \sigma_{27Al} N_{27Al}}\right)}{\lambda_{28Al}} \quad t_{irr} = 0.831 \cdot \text{sec}$$

This is a practically achievable irradiation time with a rapid rabbit system.

$$N_{115In} := \frac{R_{116In}}{\phi \sigma_{115In} (1 - \exp(-\lambda_{116In} t_{irr}))} \quad N_{115In} = 5.512 \cdot 10^{18}$$

$$m_{In} := N_{115In} \frac{M_{wIn}}{N_A \cdot X_{In}} \quad m_{In} = 1.098 \cdot 10^{-6} \cdot \text{kg} \quad 100 \cdot \frac{m_{In}}{m_{tot}} = 1.098 \quad \%$$

$i := 1..9$  The sensitivity is only marginally worse, but the irradiation time is long enough to be practical.

$$R_{In_i} := 10^i$$

$R_{In_i}$	$MDA_i :=$	$t_i :=$
10	1.078	$8.296 \cdot 10^{-7}$
100	1.078	$8.296 \cdot 10^{-6}$
$1 \cdot 10^3$	1.078	$8.296 \cdot 10^{-5}$
$1 \cdot 10^4$	1.078	$8.296 \cdot 10^{-4}$
$1 \cdot 10^5$	1.08	0.008
$1 \cdot 10^6$	1.098	0.083
$1 \cdot 10^7$	1.294	0.831
$1 \cdot 10^8$	4.452	8.462
$1 \cdot 10^9$		105.112

MDA = Minimum Detectable Amount (%)  
R = Indium activity (Bq)  
t = Irradiation time (s)



